## OPTIMIZATION OF HYBRID SYSTEM WITH VARYING INITIAL STATE

## N.V. Balashevich<sup>1</sup>, Louadj Kahina<sup>2</sup>

<sup>1</sup> Institute of Mathematics, National Academy of Sciences of Belarus

11 Surganov str., 220072 Minsk, Belarus balash@im.bas-net.by

Mouloud Mammeri University of Tizi-Ouzou BP 17 RP 15000, Tizi-Ouzou, Algeria louadj\_kahina@yahoo.fr

Hybrid system under consideration belongs to the class of switched linear autonomous systems which characterizes by multiple modes for system's dynamics and switching conditions described transitions between the modes [1]:

$$\dot{x} = A_i x + b_i u, \quad \theta_{i-1} \le t < \theta_i, \ i = \overline{1, L},$$

$$h'_i x(\theta_i) = g_i, \ i = \overline{1, L},$$

$$0 = \theta_0 < \theta_1 < \dots < \theta_{L-1} < \theta_L = t^*,$$

where  $x, b_i, h_i \in \mathbb{R}^n$ ,  $u, g_i \in \mathbb{R}$ ,  $A_i \in \mathbb{R}^{n \times n}$ ,  $i = \overline{1, L}$ ;  $T = [0, t^*]$  is a control interval.

As accessible controls discrete functions  $u(t) = u(\tau)$ ,  $\tau \in T_h = \{0, h, \dots, t^* - h\}$ , are considered, where  $h = t^*/N$  is a sampling period, N is an integer.

The problem is to maximize a value of the linear endpoint performance index over initial state  $x_0$ , bounded control function  $u(\cdot) = (u(t), t \in T)$ , and switching instants  $\theta = (\theta_1, \dots, \theta_{L-1})$ :

$$J(x_0, u(\cdot), \theta) = c'x(t^*) \longrightarrow \max,$$

$$\dot{x} = A_i x + b_i u, \ t \in [\theta_{i-1}, \theta_i), \ i = \overline{1, L},$$

$$x(0) = x_0 \in X_0 = \{ z \in R^n : Gz \le \delta, d_* \le z \le d^* \},$$

$$h'_i x(\theta_i) = g_i, \ i = \overline{1, L}, \quad |u(t)| \le 1, \ t \in T,$$

$$(1)$$

where  $X_0$  is a set of admissible initial states,  $G \in \mathbb{R}^{k \times n}$ .

Algorithms of constructing open-loop and closed-loop solutions to problem (1) are suggested. The algorithm of open-loop optimization of systems (1) is based on the approach to the solution of linear optimal control problems with the use of advanced linear programming technique [2].

Constructing of positional solution to problem (1) is investigated in the framework of the approach to the optimal synthesis problem [2, 3] based on real-time correction of open-loop solutions subject to small variations of current position. Features of the algorithm of realization of positional solution to problem (1) are discussed.

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## References

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