

STABILIZATION OF A CLASS OF HYPERBOLIC SYSTEMS COUPLED WITH INTEGRO-DIFFERENTIAL EQUATIONS

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Consider a hyperbolic system of the form

$$\frac{\partial w(x, t)}{\partial t} + G(x, c) \frac{\partial w(x, t)}{\partial x} = \psi(x)w(x, t), \quad w(x, t) \in \mathbb{R}^n, \quad x \in [0, l], \quad t \geq 0, \quad (1)$$

subject to the boundary conditions

$$w_i(0, t) = B_i(c)/G_i(0, c), \quad (B_i \geq 0, \quad G_i > 0, \quad i = 1, 2, \dots, n), \quad (2)$$

where the function $c = c(t)$ is defined by

$$\frac{dc(t)}{dt} = F \left(c(t), \int_0^l \phi(x)w(x, t)dx, u \right), \quad (3)$$

and u is treated as the control. The above control system was studied as a mathematical model of the continuous crystallization process ($n = 1$) or preferential crystallization of two enantiomers ($n = 2$) in [1], where information about the physical meaning of its state variables and coefficients was also presented.

In this talk, we present a new control design scheme to stabilize the equilibrium of system (1)–(3) by means of a state feedback law for different values of n .

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References

1. *Sklyar G., Zuyev A. (Eds.) Stabilization of Distributed Parameter Systems: Design Methods and Applications.* Springer, 2021.